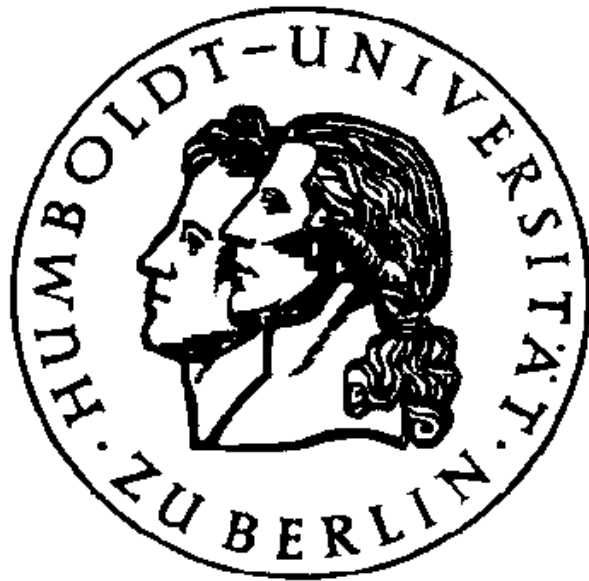
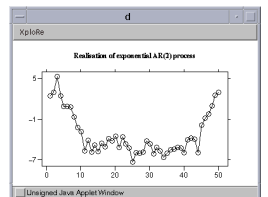


Web quantlets for time series analysis



Wolfgang Härdle, Torsten Kleinow, Rolf Tschernig
([this paper online as pdf](#))

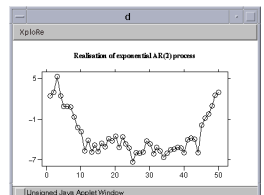


1. Introduction

*“Empower people through great software
anytime, anywhere and on any device”*

Bill Gates

*“Empower statisticians through great methods
anytime, anywhere and on any device”*

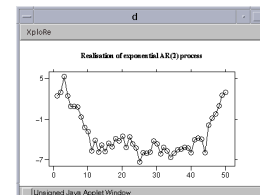


New Methods in Time Series Analysis involve often

- complex computing algorithms
- hard mathematical problems

Example: nonparametric time series analysis

$$Y_t = f(Y_{t-i_1}, Y_{t-i_2}, \dots, Y_{t-i_m}) + \sigma(Y_{t-i_1}, Y_{t-i_2}, \dots, Y_{t-i_m})\xi_t$$



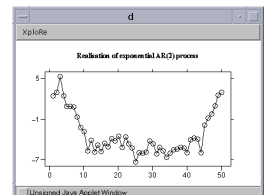
Example (ctd.)

$$Y_t = f(Y_{t-i_1}, Y_{t-i_2}, \dots, Y_{t-i_m}) + \sigma(Y_{t-i_1}, Y_{t-i_2}, \dots, Y_{t-i_m})\xi_t$$

- computational difficulty: lag selection
- mathematical difficulty: nonparametric smoothing

Method of CAFPE solves this problem but is computationally and mathematically difficult. It is, however, very interesting for detection of new models, see e.g.

Tschernig, R. & Yang, L. (2000), 'Nonparametric lag selection for time series', Journal of Time Series Analysis.



Solutions:

do it yourself



telephone



email

help.me@colleague

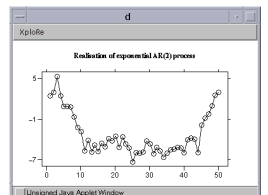
method cemetery



Java



Web Quantlets



Plan of talk

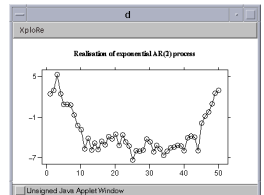
✓ 1. Introduction

2. Nonparametric identification of nonlinear time series models

3. Web quantlets

4. Illustration

5. 



2. Nonparametric identification of nonlinear time series models

Nonlinear conditional heteroskedastic autoregressive time series process

$$Y_t = f(\mathbf{X}_t) + \sigma(\mathbf{X}_t)\xi_t, \quad t = 0, 1, \dots,$$

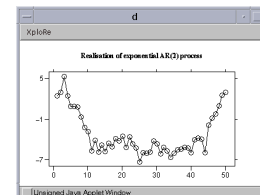
with

$$\mathbf{X}_t = (Y_{t-i_1}, Y_{t-i_2}, \dots, Y_{t-i_m})^T$$

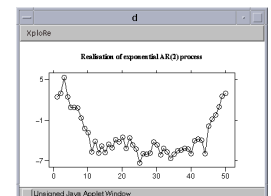
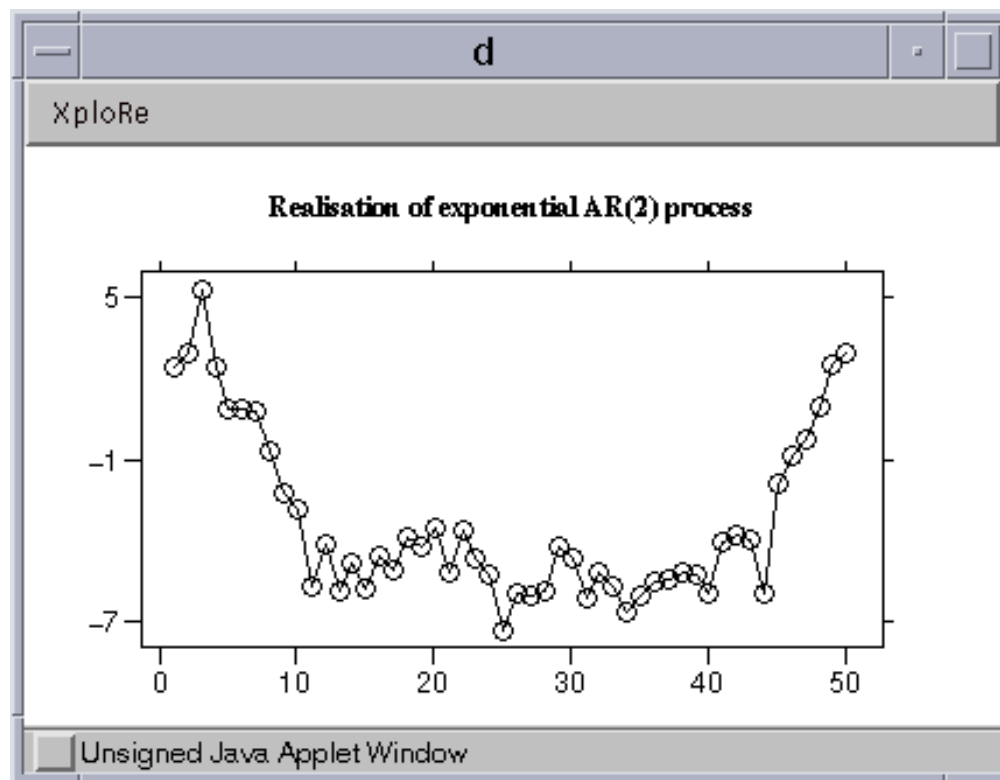
and

$$\xi_t \text{ i.i.d, } E[\xi_t] = 0, \quad E[\xi_t^2] = 1$$

used in establishing new time series models



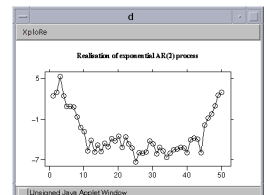
Nonparametric identification of nonlinear time series models



Nonparametric identification of nonlinear time series models

requires two steps:

- 1) **lag selection:** choose the relevant lags $i_1, \dots, i_m$ including their number m for the autoregression function f and the conditional standard deviation σ .
- 2) **function estimation:** estimate f and, if desired, σ for the chosen lag vector.



Step 2: Function estimation

For given set of lags: $i_1, i_2, \dots, i_m$:

Local linear function estimation $\hat{f}(\mathbf{x}, h) = \hat{c}_0$

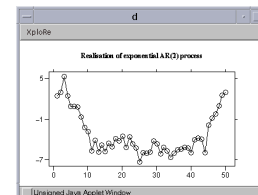
$$\{\hat{c}_0, \hat{\mathbf{c}}\} = \arg \min_{\{c_0, \mathbf{c}\}}$$

$$\sum_{t=1}^T \{Y_t - c_0 - (\mathbf{X}_t - \mathbf{x})^T \mathbf{c}\}^2 K_h(\mathbf{X}_t - \mathbf{x})$$

with product kernel

$$K_h(\mathbf{X}_t - \mathbf{x}) = h^{-m} \prod_{i=1}^m K \{(X_{t,i} - x_i)/h\}$$

(Härdle & Tsybakov, 1997)



Step 2: Function estimation - bandwidth choice

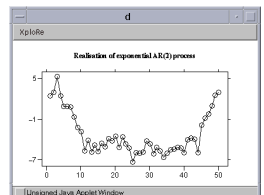
Final Prediction Error (FPE)

$$FPE(h, i_1, \dots, i_m) = E \left[\left(\check{Y}_t - \hat{f}(\check{X}_t, h) \right)^2 w(\check{X}_{t,M}) \right]$$

where $\check{X}_{t,M} = (\check{Y}_{t-1}, \dots, \check{Y}_{t-M})^T$.

Under appropriate conditions it holds that

$$FPE(h) = AFPE(h) + o\{h^4 + T^{-1}h^{-m}\}$$



Asymptotic Final Prediction Error

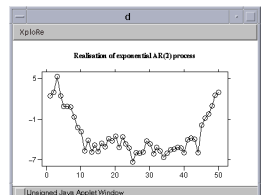
Under appropriate conditions it holds that

$$FPE(h) = AFPE(h) + o\{h^4 + T^{-1}h^{-m}\}$$

where

$$AFPE(h) = A + b(h)B + c(h)C$$

$$\text{Asymp. FPE} = \int \text{Var} + \int \widehat{\text{Var}}(\hat{f}) + \int \widehat{\text{bias}}(\hat{f})^2$$



Step 2: Function estimation - bandwidth choice

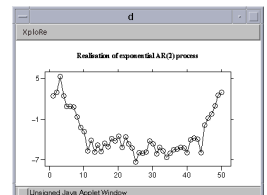
Plug-in bandwidth

Estimate asymptotically optimal bandwidth

$$h_{opt} = \left(d(T, m, K(\cdot)) \frac{B}{C} \right)^{\frac{1}{m+4}}$$

by estimating B and C

e.g. by using direct local quadratic estimators for C (Yang & Tschernig, 1999)



Step 1: Lag selection (Tschernig & Yang, 2000)

Estimated Asymptotic FPE

$$AFPE = \hat{A}(\hat{h}_{opt}) + 2K(0)^m T^{-1} \hat{h}_{opt}^{-m} \hat{B}(\hat{h}_B)$$

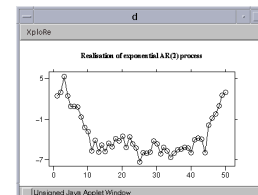
Estimated Corrected Asymptotic FPE (CAFPE)

$$CAFPE = AFPE \left\{ 1 + mT^{-4/(m+4)} \right\}$$

Select lag vector with smallest *AFPE* or *CAFPE*.

Both criteria are consistent, e.g.

$$Pr \left(\hat{m} = m, \hat{i}_s = i_s, s = 1, 2, \dots, m \right) \xrightarrow{T \rightarrow \infty} 1.$$



Step 1: Lag selection - Details

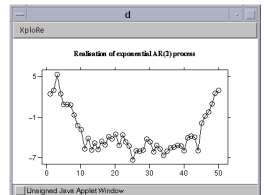
Details of *AFPE* estimator

$$\hat{A}(h) = T^{-1} \sum_{t=1}^T \left\{ y_t - \hat{f}(\mathbf{X}_t, h) \right\}^2 w(\mathbf{X}_{t,M})$$

$$\hat{B}(\hat{h}_B) = T^{-1} \sum_{t=1}^T \left\{ Y_t - \hat{f}(\mathbf{X}_t, \hat{h}_B) \right\}^2 \frac{w(\mathbf{X}_{t,M})}{\hat{\mu}(\mathbf{X}_t, \hat{h}_B)}$$

and rule-of-thumb bandwidth

$$\hat{h}_B = \hat{\sigma} \left(\frac{4}{T+2} \right)^{1/(m+4)} T^{-1/(m+4)}$$

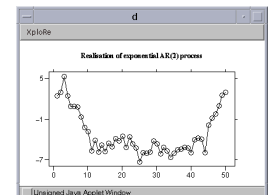


3. Web Quantlets

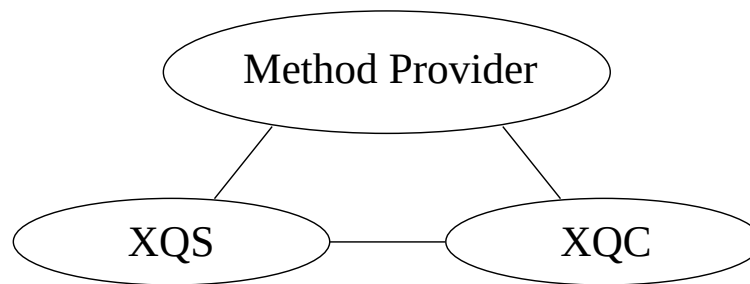
- Java applets
 - VESTAC project at KU Leuven
 - statlab Heidelberg
 - and many others
- Statistical programming language macros
 - StatLib
 - and many other professional sites

These are extremal positions.

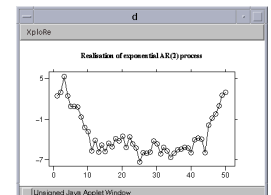
We propose a “statistical middleware” solution based on a Client/Server concept.



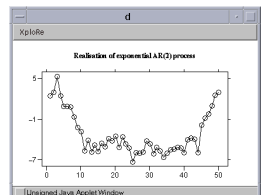
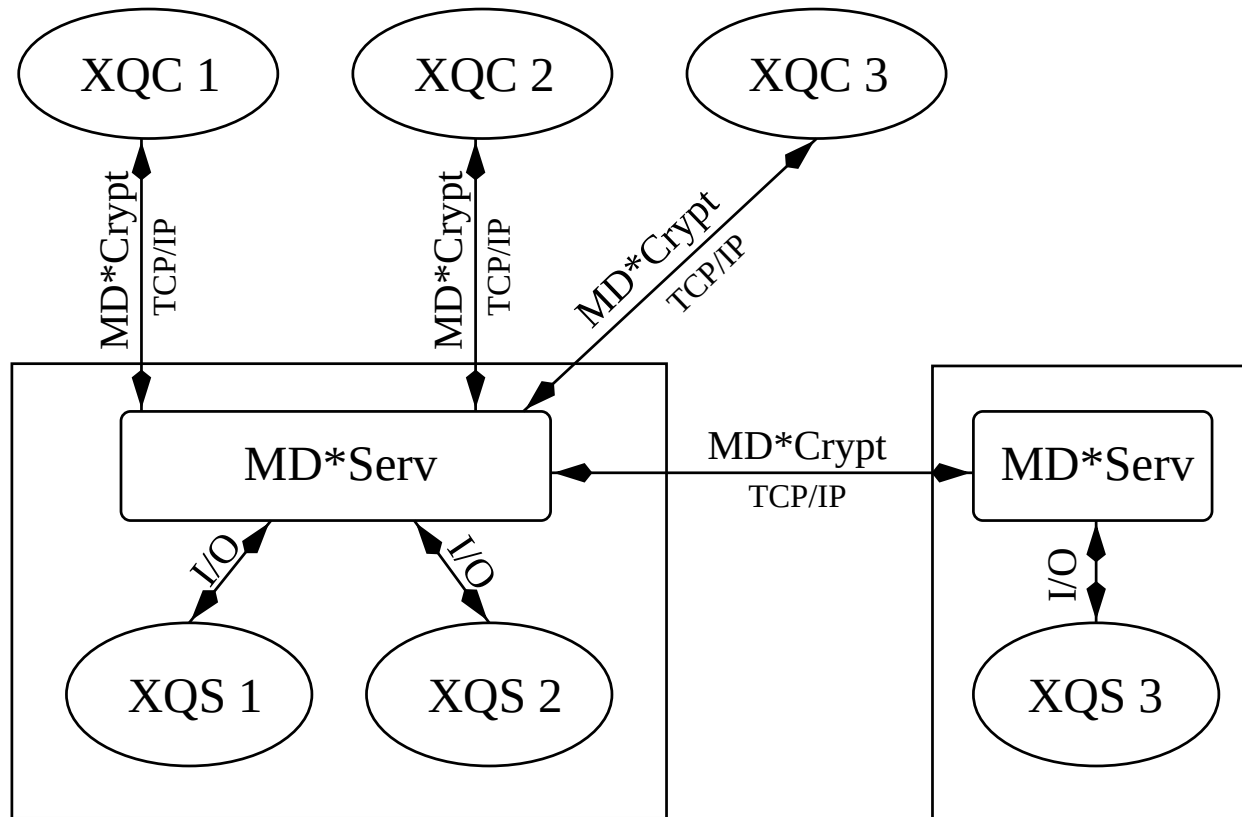
Basic Architecture



- client (XQC): student, scientist
- method provider: university, MD*Tech center
- server (XQS): university, private institution



Technical background



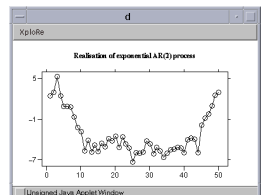
Elements of XQS/XQC

XQC client program, GUI, running on user's machine, depending on particular interests

MD***Crypt** protocol for communication

MD***Serv** middleware, manages the XQS/XQC communication

XQS server, provides statistical computing power



4. Illustration

- generate nonlinear time series data
- conduct nonparametric model identification
- present lag selection results
- do all via the XQS/XQC architecture

The example

- is contained in the  `cafpeexample` which is written in the statistical language XploRe
- can be edited and executed from any standard Webbrowser

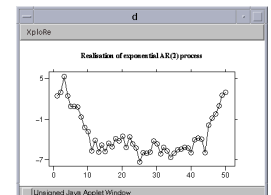


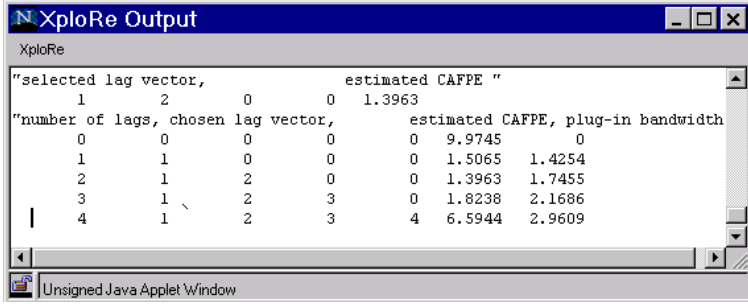
Illustration - lag selection

- generate 50 observations of exponential autoregressive process

$$Y_t = 0.3Y_{t-1} + 0.6Y_{t-2} + (1.9Y_{t-1} - 1.1Y_{t-2}) \exp(-0.1 * Y_{t-1}^2) + \xi_t$$

using  **genexpar** where ξ_t is standardnormal

- compute *CAFPE* for all lag combinations up to four lags and highest lag 4 using  **cafpe**.



XploRe Output

XploRe

"selected lag vector,				estimated CAFPE "
1	2	0	0	1.3963

"number of lags, chosen lag vector,				estimated CAFPE, plug-in bandwidth
0	0	0	0	0 9.9745 0
1	1	0	0	0 1.5065 1.4254
2	1	2	0	0 1.3963 1.7455
3	1	2	3	0 1.8238 2.1686
4	1	2	3	4 6.5944 2.9609

Unsigned Java Applet Window

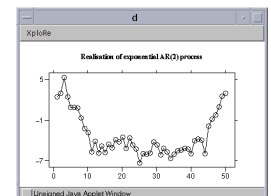


Illustration - function estimation

The  `plotloclineexample` allows to estimate and to plot the conditional function f for the selected lags 1 and 2 and the obtained plug-in bandwidth h_{opt}

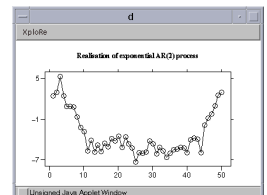
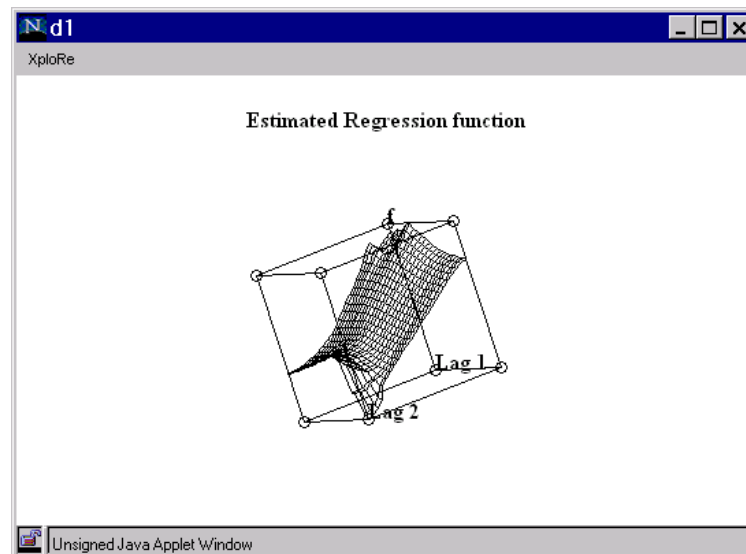
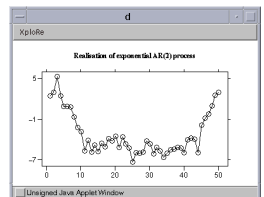


Illustration - advantages of the XQS/XQC architecture

- client's machine is left for client's work
- Example: For $T = 5000$ the example program would take 10.5 hours on a 200 Mhz Pentium in contrast to 2.5 on the Sun Ultra 2 Sparc server.

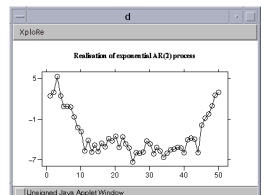


5.

Cooperation with Springer Verlag, Heidelberg

 has the following components

- classical printed book
- CD with book and slides
- options for updates
- option for XQS





Statistics of financial markets

- book of 300 pages
- CD with
 - pdf/ps/html version
 - MS Windows XQS
 - Java XQC
 - all necessary Quantlets
 - book update rights ≤ 2 years
 - APSS (auto pilot support system)

(userid: finanz password: mathe)

