

Some information inequalities for statistical inference

K. V. Harsha^{1,2} · Alladi Subramanyam¹

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Abstract

In this paper, we first describe the generalized notion of Cramer–Rao lower bound obtained by Naudts (J Inequal Pure Appl Math 5(4), Article 102, 2004) using two families of probability density functions: the original model and an escort model. We reinterpret the results in Naudts (2004) from a statistical point of view and obtain some interesting examples in which this bound is attained. Further, we obtain information inequalities which generalize the classical Bhattacharyya bounds in both regular and non-regular cases.

Keywords Information inequality \cdot Generalized Cramer–Rao bound \cdot Escort probability distribution \cdot Generalized Bhattacharyya bounds \cdot Deformed exponential family

☑ K. V. Harsha harshakv@math.iitb.ac.in; kv.harsha1989@gmail.com

Alladi Subramanyam as@math.iitb.ac.in

¹ Department of Mathematics, Indian Institute of Technology Bombay, Powai, Mumbai 400076, India

² Present Address: Madrid, Spain