



# On univariate slash distributions, continuous and discrete

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## Abstract

In this article, I explore in a unified manner the structure of uniform slash and  $\alpha$ -slash distributions which, in the continuous case, are defined to be the distributions of  $Y / U$  and  $Y_\alpha / U^{1/\alpha}$  where  $Y$  and  $Y_\alpha$  follow any distribution on  $\mathbb{R}^+$  and, independently,  $U$  is uniform on  $(0, 1)$ . The parallels with the monotone and  $\alpha$ -monotone distributions of  $Y \times U$  and  $Y_\alpha \times U^{1/\alpha}$ , respectively, are striking. I also introduce discrete uniform slash and  $\alpha$ -slash distributions which arise from a notion of negative binomial thinning/fattening. Their specification, although apparently rather different from the continuous case, seems to be a good one because of the close way in which their properties mimic those of the continuous case.

**Keywords** Binomial thinning · Monotone density · Negative binomial fattening · Uniform random variable

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