

# Quantile regression based on counting process approach under semi-competing risks data

Jin-Jian Hsieh<sup>1</sup> · Hong-Rui Wang<sup>1</sup>

Received: 1 December 2015 / Revised: 4 October 2016 / Published online: 31 December 2016  
© The Institute of Statistical Mathematics, Tokyo 2016

**Abstract** In this paper, we investigate the quantile regression analysis for semi-competing risks data in which a non-terminal event may be dependently censored by a terminal event. The estimation of quantile regression parameters for the non-terminal event is complicated. We cannot make inference on the non-terminal event without extra assumptions. Thus, we handle this problem by assuming that the joint distribution of the terminal event and the non-terminal event follows a parametric copula model with unspecified marginal distributions. We use the stochastic property of the martingale method to estimate the quantile regression parameters under semi-competing risks data. We also prove the large sample properties of the proposed estimator, and introduce a model diagnostic approach to check model adequacy. From simulation results, it shows that the proposed estimator performs well. For illustration, we apply our proposed approach to analyze a real data.

**Keywords** Copula model · Dependent censoring · Quantile regression · Semi-competing risks data

---

✉ Jin-Jian Hsieh  
jjhsieh@math.ccu.edu.tw

<sup>1</sup> Department of Mathematics, National Chung Cheng University, 168, University Rd., Min-Hsiung, Chia-Yi, Taiwan ROC