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The generality of the zero-one laws

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Abstract We prove game-theoretic generalizations of some well-known zero-one laws. Our proofs make the martingales behind the laws explicit, and our results illustrate how martingale arguments can have implications going beyond measure-theoretic probability.

Keywords Game-theoretic probability · Invariant event · Martingale · Permutable event · Tail event · Upper probability