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ESTIMATING THE COVARIANCE MATRIX AND THE GENERALIZED VARIANCE UNDER A SYMMETRIC LOSS TATSUYA KUBOKAWA^{*} AND YOSHIHIKO KONNO

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Abstract. For estimating the power of a generalized variance under a multivariate normal distribution with unknown means, the inadmissibility of the best affine equivariant estimator relative to the symmetric loss is shown, and a class of improved estimators is given. The problem of estimating the covariance matrix is also discussed.

Key words and phrases: Covariance matrix, generalized variance, Wishart distribution, affine equivariant estimators, Stein's truncated estimator, inadmissibility.