

## Jackknife empirical likelihood for the difference of two volumes under ROC surfaces

Yueheng An<sup>1</sup> · Yichuan Zhao<sup>1</sup>

Received: 12 January 2016 / Revised: 28 November 2016 / Published online: 15 November 2017 © The Institute of Statistical Mathematics, Tokyo 2017

**Abstract** The volume under a surface (VUS) is an effective measure for evaluating the discriminating power of a diagnostic test with three ordinal diagnostic groups. In this paper, we investigate the difference of two correlated VUS's to compare two treatments for discrimination of three-class classification data. A jackknife empirical likelihood (JEL) procedure is employed to avoid the variance estimation in the existing methods. We prove that the limiting distribution of the empirical log-likelihood ratio statistic follows a  $\chi^2$  distribution. Extensive numerical studies show that the JEL confidence intervals outperform those based on the normal approximation method. The proposed method is also applied to the Alzheimer's disease data.

**Keywords** Jackknife empirical likelihood · Receiver operating characteristic (ROC) curve · Volume under an ROC surface

Department of Mathematics and Statistics, Georgia State University, Atlanta, GA 30303, USA



 <sup>∑</sup> Yichuan Zhao yichuan@gsu.edu