

Asymptotic moving average representation of high-frequency sampled multivariate CARMA processes

Péter Kevei¹

Received: 22 April 2016 / Revised: 8 December 2016 / Published online: 20 February 2017
© The Institute of Statistical Mathematics, Tokyo 2017

Abstract High-frequency sampled multivariate continuous time autoregressive moving average processes are investigated. We obtain asymptotic expansion for the spectral density of the sampled MCARMA process $(Y_{n\Delta})_{n \in \mathbb{Z}}$ as $\Delta \downarrow 0$, where $(Y_t)_{t \in \mathbb{R}}$ is an MCARMA process. We show that the properly filtered process is a vector moving average process, and determine the asymptotic moving average representation of it, thus generalizing the univariate results to the multivariate model. The determination of the moving average representation of the filtered process, important for the analysis of high-frequency data, is difficult for any fixed positive Δ . However, the results established here provide a useful and insightful approximation when Δ is very small.

Keywords Multivariate continuous time autoregressive moving average (CARMA) process · Spectral density · High-frequency sampling · Discretely sampled process

This research was funded by a postdoctoral fellowship of the Alexander von Humboldt Foundation.

✉ Péter Kevei
peter.kevei@tum.de

¹ Center for Mathematical Sciences, Technische Universität München, Boltzmannstraße 3, 85748 Garching, Germany