

## Testing the constancy of Spearman's rho in multivariate time series

Ivan Kojadinovic $^1 \cdot Jean-François Quessy^2 \cdot Tom Rohmer^3$ 

Received: 14 July 2014 / Revised: 9 January 2015 / Published online: 1 May 2015 © The Institute of Statistical Mathematics, Tokyo 2015

**Abstract** A class of tests for change-point detection designed to be particularly sensitive to changes in the cross-sectional rank correlation of multivariate time series is proposed. The derived procedures are based on several multivariate extensions of Spearman's rho. Two approaches to carry out the tests are studied: the first one is based on resampling and the second one consists of estimating the asymptotic null distribution. The asymptotic validity of both techniques is proved under the null for strongly mixing observations. A procedure for estimating a key bandwidth parameter involved in both approaches is proposed, making the derived tests parameter-free. Their finite-sample behavior is investigated through Monte Carlo experiments. Practical recommendations are made and an illustration on trivariate financial data is finally presented.

Jean-François Quessy jean-francois.quessy@uqtr.ca

Tom Rohmer tom.rohmer@univ-nantes.fr

- <sup>1</sup> Laboratoire de mathématiques et applications, UMR CNRS 5142, Université de Pau et des Pays de l'Adour, B.P. 1155, 64013 Pau Cedex, France
- <sup>2</sup> Département de mathématiques et d'informatique, Université du Québec à Trois-Rivières, C.P. 500, Trois-Rivières, QC G9A 5H7, Canada
- <sup>3</sup> Laboratoire de mathématiques Jean Leray, Université de Nantes, B.P. 92208, 44322 Nantes Cedex 3, France

**Electronic supplementary material** The online version of this article (doi:10.1007/s10463-015-0520-2) contains supplementary material, which is available to authorized users.

<sup>☑</sup> Ivan Kojadinovic ivan.kojadinovic@univ-pau.fr

**Keywords** Change-point detection  $\cdot$  Empirical copula  $\cdot$  HAC kernel variance estimator  $\cdot$  Multiplier central limit theorems  $\cdot$  Partial-sum processes  $\cdot$  Ranks  $\cdot$  Spearman's rho  $\cdot$  Strong mixing