## Estimating the ratio of two scale parameters: a simple approach

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Received: 30 November 2009 / Revised: 17 May 2010 / Published online: 31 July 2010 © The Institute of Statistical Mathematics, Tokyo 2010

**Abstract** We describe a simple approach for estimating the ratio  $\rho = \sigma_2/\sigma_1$  of the scale parameters of two populations from a decision theoretic point of view. We show that if the loss function satisfies a certain condition, then the estimation of  $\rho$  reduces to separately estimating  $\sigma_2$  and  $1/\sigma_1$ . This implies that the standard estimator of  $\rho$  can be improved by just employing an improved estimator of  $\sigma_2$  or  $1/\sigma_1$ . Moreover, in the case where the loss function is convex in some function of its argument, we prove that such improved estimators of  $\rho$  are further dominated by corresponding ones that use all the available data. Using this result, we construct new classes of double-adjustment improved estimators for several well-known convex as well as non-convex loss functions. In particular, Strawderman-type estimators of  $\rho$  in general models are given whereas Shinozaki-type estimators of the ratio of two normal variances are briefly treated.

**Keywords** Decision theory  $\cdot$  Improved estimation of a scale parameter  $\cdot$  Improved estimation of ratio of scale parameters  $\cdot$  Stein's and Brewster and Zidek's techniques  $\cdot$  Strawderman's technique  $\cdot$  Kubokawa's approach