Bivariate Fibonacci polynomials of order k with statistical applications

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Abstract In the present article, we investigate the properties of bivariate Fibonacci polynomials of order k in terms of the generating functions. For k and ℓ ($1 \le \ell \le k-1$), the relationship between the bivariate Fibonacci polynomials of order k and the bivariate Fibonacci polynomials of order ℓ is elucidated. Lucas polynomials of order k are considered. We also reveal the relationship between Lucas polynomials of order k and Lucas polynomials of order ℓ . The present work extends several properties of Fibonacci and Lucas polynomials of order k, which will lead us a new type of geneses of these polynomials. We point out that Fibonacci and Lucas polynomials of order k are closely related to distributions of order k and show that the distributions possess properties analogous to the bivariate Fibonacci and Lucas polynomials of order k.

Keywords Fibonacci polynomials \cdot Lucas polynomials \cdot Success runs \cdot Waiting time \cdot Distributions of order k \cdot Probability generating function \cdot Continued fraction