

## The geometry of the Wilks's $\Lambda$ random field

F. Carbonell · K. J. Worsley · L. Galan

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**Abstract** The statistical problem addressed in this paper is to approximate the  $P$  value of the maximum of a smooth random field of Wilks's  $\Lambda$  statistics. So far results are only available for the usual univariate statistics  $(Z, t, \chi^2, F)$  and a few multivariate statistics (Hotelling's  $T^2$ , maximum canonical correlation, Roy's maximum root). We derive results for any differentiable scalar function of two independent Wishart random fields, such as Wilks's  $\Lambda$  random field. We apply our results to a problem in brain shape analysis.

**Keywords** Multivariate random fields · Excursion sets · Euler characteristic · Derivatives of matrix functions