KERNEL ESTIMATION FOR STATIONARY DENSITY OF MARKOV CHAINS WITH GENERAL STATE SPACE

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Abstract. Let $\{X_n\}_{n\geq 0}$ be a Markov chain with stationary distribution $f(x)\nu(dx)$, ν being a σ -finite measure on $E \subset \mathbb{R}^d$. Under strict stationarity and mixing conditions we obtain the consistency and asymptotic normality for a general class of kernel estimates of $f(\cdot)$. When the assumption of stationarity is dropped these results are extended to geometrically ergodic chains.

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