

ON CHARACTERIZATION OF POWER SERIES DISTRIBUTIONS BY A MARGINAL DISTRIBUTION AND A REGRESSION FUNCTION

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Abstract. The conditional distribution of Y given $X = x$, where X and Y are non-negative integer-valued random variables, is characterized in terms of the regression function of X on Y and the marginal distribution of X which is assumed to be of a power series form. Characterizations are given for a binomial conditional distribution when X follows a Poisson, binomial or negative binomial, for a hypergeometric conditional distribution when X is binomial and for a negative hypergeometric conditional distribution when X follows a negative binomial.

Key words and phrases: Characterizations, regression function, Poisson, binomial, negative binomial, hypergeometric.