

## CLOSER ESTIMATORS OF A COMMON MEAN IN THE SENSE OF PITMAN

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**Abstract.** Consider the problem of estimating the common mean of two normal populations with different unknown variances. Suppose a random sample of size  $m$  is drawn from the first population and a random sample of size  $n$  is drawn from the second population. The paper gives a family of estimators closer than the sample mean of the first population in the sense of Pitman (1937, *Proc. Cambridge Phil. Soc.*, **33**, 212-222). In particular, the Graybill-Deal estimator (1959, *Biometrics*, **15**, 543-550) is shown to be closer than each of the sample means if  $m \geq 5$  and  $n \geq 5$ .

*Key words and phrases:* Pitman closeness, common mean, Graybill-Deal estimator.