

# AN APPLICATION OF THE CONVOLUTION INEQUALITY FOR THE FISHER INFORMATION

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**Abstract.** A characterization of the normal distribution by a statistical independence on a linear transformation of two mutually independent random variables is proved by using the convolution inequality for the Fisher information.

*Key words and phrases:* The Fisher information, convolution inequality, statistical independence, characterization of the normal distribution.