

## NONPARAMETRIC CONFIDENCE INTERVALS FOR FUNCTIONS OF SEVERAL DISTRIBUTIONS

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**Abstract.** Let  $F = (F_1 \cdots F_k)$  denote  $k$  unknown distribution functions and  $\hat{F} = (\hat{F}_1 \cdots \hat{F}_k)$  their sample (empirical) functions based on random samples from them of sizes  $n_1, \dots, n_k$ . Let  $T(F)$  be a real functional of  $F$ . The cumulants of  $T(\hat{F})$  are expanded in powers of the inverse of  $n$ , the minimum sample size. The Edgeworth and Cornish-Fisher expansions for both the standardized and Studentized forms of  $T(\hat{F})$  are then given together with confidence intervals for  $T(F)$  of level  $1 - \alpha + O(n^{-j/2})$  for any given  $\alpha$  in  $(0, 1)$  and any given  $j$ . In particular, confidence intervals are given for linear combinations and ratios of the means and variances of different populations without assuming any parametric form for their distributions.

*Key words and phrases:* Confidence interval, nonparametric, Cornish-Fisher expansions, functional derivatives.